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## Prime vs. Prime Cube Action, Part 1: Basic Reference Positions

06 Oct 2010
by Matt Cohn-Geier
The most complex positions in backgammon are prime vs. prime. Typically, one player has a clear advantage, however, how much of one is difficult to quantify. Sometimes it involves winning many gammons even though the game might be close to a toss up. A small change to a position can make an enormous difference. Even the best players struggle to understand these positions and frequently make huge mistakes. I'm going to try to tackle some of these problems and look at the various factors that go into cube action.


Matt Cohn-Geier

Tackling prime vs. prime positions is more difficult than one might imagine. If it's difficult for expert players to understand, it must be really difficult to teach. To bridge the gap, I'm going to go back to one of my favorite pastimes, looking at a variety of borderline reference positions and trying to draw some conclusions between them. This month, we're going to look at very pure situations: trying to leap a solid 5 prime while having a 6 prime of one's own. Next month, we'll tackle some more impure situations that are more likely to come up OTB.

Don't worry if you can't remember whether one of the positions is a double or not, or a take or not. As long as you can remember that they are on the edge then you can infer much more about a whole class of position-types.

A lot of people have asked me questions about how I study backgammon, about why reference positions are important, about why borderline positions are important, about what kinds of reference positions to study, and everything else under the sun. Hopefully this article will help to shed some light on what it is that an expert player can do to improve his game, if he has the desire.

A word about timing: Though in the past I and others have referred to the pips of timing left it would take to advance everyone to the ace point (or to just in front of the opponent's anchor, etc.), I'm just going to refer to it by straight pip count. I have no idea if this will be more accurate or less accurate (although my guess would be less accurate) but it will be easier for me to remember.

All positions are for money games WITHOUT Jacoby. Since most doubles in these kinds of positions are going to be redoubles (or centered cubes in a match), I want to investigate the difference between a centered double and a redouble, not the effect that Jacoby and activating gammons has on the cube action. That is more of a specialized subject unto itself.

So, without further ado, let's begin.

## Position 1A:



Let's start with something that everyone should know, and is simple and easy to remember. White has one checker on the bar against a closed board, Black is behind a 5 prime and needs to roll a 6 or crash his board. This position is a borderline double/no double with a centered cube.

[^0]Position 1B:


How much difference can a pip make? Well, if we give Black a spare on his 3 point (i.e., almost all rolls are the same but 32 keeps a closed board), now it becomes a big double.

```
Analyzed in Rollout
No Double
Player Winning Chances: 60.23% (G: 1.49% B: 0.01%)
Opponent Winning Chances:39.77% (G: 1.78% B: 0.05%)
Double/Take
Player Winning Chances: 60.45% (G: 1.56% B: 0.02%)
Opponent Winning Chances:39.55% (G: 1.72% B: 0.05%)
Cubeless Equities
No Double: +0.202
Double: +0.414
Cubeful Equities
No Double: +0.168 (-0.054)
Double/Take: +0.222
Double/Drop: +1.000 (+0.778)
Best Cube action: Double / Take
Rollout details
2 5 9 2 \text { Games rolled with Variance Reduction.}
Dice Seed: }13492
Moves and cube decisions: 3 ply
Confidence No Double: }\quad\pm0.005(+0.163...+0.172
Confidence Double: }\quad\pm0.007(+0.215\ldots+0.229
Double Decision confidence: 100.0%
Double Decision confidence: 100.0%
Duration: 49.5 seconds
```


## Position 1C:



What about if the spares were on the 5 and 1 rather than the 4 and 2? Barely a difference here.

```
Analyzed in Rollout
No Double
Player Winning Chances: 59.59% (G: 1.25% B: 0.01%)
Opponent Winning Chances:40.41% (G: 2.21% B: 0.06%)
Double/Take
Player Winning Chances: 59.51% (G: 1.43% B: 0.02%)
Opponent Winning Chances:40.49% (G: 2.19% B: 0.06%)
Cubeless Equities
No Double: +0.182
Double: +0.364
Cubeful Equities
No Double: +0.144
Double/Take: +0.141 (-0.002)
Double/Drop: +1.000 (+0.856)
Best Cube action: No Double / Take
Rollout details
2592 Games rolled with Variance Reduction.
Dice Seed: }13492
Moves and cube decisions: 3 ply
Confidence No Double: }\quad\pm0.005(+0.139...+0.148
Confidence Double: }\quad\pm0.009(+0.132\ldots+0.150
Double Decision confidence:68.2%
Take Decision confidence: 100.0%
Duration: 51.9 seconds
```


## Position 1D:



With spares on the 5 and 2 , it is a cube, but not nearly as big as spares on the 4 and 3. As we'll see later, this is one of the few instances where having a spare on the 5 point is actually worse than the alternative configuration.

| Analyzed in Rollout |  |
| :---: | :---: |
| No Double |  |
| Player Winning Chances: | 60.54\% (G: $1.32 \%$ B: 0.01\%) |
| Opponent Winning Chances:39.46\% (G: $2.20 \%$ B: $0.06 \%$ )Double/Take |  |
|  |  |
| Player Winning Chances | 60.41\% (G: 1.54\% B: 0.02 |
| Opponent Winning Chances:39.59\% (G: $2.17 \%$ B: $0.06 \%$ ) |  |
| Cubeless Equities |  |
| No Double: | +0.202 |
| Double: | +0.403 |
| Cubeful Equities |  |
| No Double: | +0.162 (-0.023) |
| Double/Take: | +0.185 |
| Double/Drop: | +1.000 (+0.815) |
| Best Cube action: Double / Take |  |
| Rollout details |  |
| 2592 Games rolled with Variance Reduction. Dice Seed: 134923 |  |
|  |  |
| Moves and cube decisions: 3 ply |  |
| Confidence No Double: | $\pm 0.004$ (+0.158...+0.167) |
| Confidence Double: | $\pm 0.008(+0.177 \ldots+0.193)$ |
| Double Decision confidence: | : 100.0\% |
| Take Decision confidence: | 100.0\% |
| Duration: 1 minute 01 second |  |

## Position 1E:



With spares on the 6 and 1, not only is it clearly not a cube, it's now a beaver! With very little timing, the 6 point is the worst place to have a spare. Note that even though this position gains a pip of timing over Position 1C (ostensibly allowing Black to play rolls like 41 and 32 while keeping a closed board), it's considerably worse to have the checker on the 6 rather than the 5 .

| Analyzed in Rollout |  |
| :---: | :---: |
|  |  |
| Player Winning Chances: $\quad 58.19 \%$ (G: $1.38 \% \mathrm{~B}: 0.01 \%$ ) |  |
| Opponent Winning Chances:4 | :41.81\% (G: 4.81\% B: 0.14\%) |
| Double/Take |  |
| Player Winning Chances: | 58.34\% (G: 1.26\% B: 0.01\%) |
| Opponent Winning Chances:41.66\% (G: $4.79 \%$ B: $0.14 \%$ ) |  |
| Cubeless Equities |  |
| No Double: | +0.128 |
| Double: | +0.260 |
| Cubeful Equities |  |
| No Double: | +0.054 |
| Double/Take: | -0.042 (-0.096) |
| Double/Drop: | +1.000 (+0.946) |
| Best Cube action: No Double / Beaver |  |
| Rollout details |  |
| 2592 Games rolled with Variance Reduction. Dice Seed: 134923 |  |
|  |  |
| Moves and cube decisions: 3 ply |  |
| Confidence No Double: | $\pm 0.007$ (+0.047 ...+0.061) |
| Confidence Double: $\quad \pm 0.027(-0.069 \ldots-0.015)$ |  |
| Double Decision confidence: $100.0 \%$ |  |
| Beaver Decision confidence: $99.9 \%$ |  |
| Duration: 1 minute 18 second |  |

## Position 1F:



In fact, even with spares on the 6 and 2, it's not an initial cube. There are too many bad blotting rolls. Note the increase in the number of gammons that White wins.
Analyzed in Rollout
No Double
Player Winning Chances: 59.62\% (G: 1.42\% B: 0.01\%)
Opponent Winning Chances:40.38\% (G: 4.15\% B: 0.13\%)
Double/Take
Player Winning Chances: $\quad 59.79 \%$ (G: $1.39 \%$ B: $0.02 \%$ )
Opponent Winning Chances:40.21\% (G: 4.13\% B: 0.13\%)
Cubeless Equities
No Double: +0.164
Double: +0.335
Cubeful Equities
No Double: +0.098
Double/Take: $\quad+0.069(-0.029)$
Double/Drop: $\quad+1.000(+0.902)$
Best Cube action: No Double / Take

## Rollout details

2592 Games rolled with Variance Reduction.
Dice Seed: 134923
Moves and cube decisions: 3 ply
Confidence No Double: $\quad \pm 0.006(+0.092 \ldots+0.104)$
Confidence Double: $\quad \pm 0.012(+0.057 \ldots+0.081)$
Double Decision confidence: 100.0\%
Take Decision confidence: $100.0 \%$
Duration: 1 minute 15 seconds

## Position 1G:



Much more often the case will be that Black is holding the cube. In that case, the reference that he needs to redouble is this. Anything better than this will be a redouble, and anything worse than this won't be.

| Analyzed in Rollout |  |
| :---: | :---: |
| No Double |  |
| Player Winning Chances: $\quad 63.70 \%$ (G: $1.57 \%$ B: $0.01 \%$ )Opponent Winning Chances:36.30\% (G: $2.03 \%$ B: $0.05 \%$ ) |  |
|  |  |
| Double/Take |  |
| Opponent Winning Chances:36.00\% (G: $1.74 \%$ B: $0.05 \%$ ) |  |
|  |  |
| Cubeless Equities |  |
| No Redouble: | +0.269 |
| Redouble: | +0.558 |
| Cubeful Equities |  |
| No Redouble: | +0.348 (-0.015) |
| Redouble/Take: | +0.363 |
| Redouble/Drop: | +1.000 (+0.637) |
| Best Cube action: Redouble / Take |  |
| Rollout details |  |
| 2592 Games rolled with Variance Reduction.Dice Seed: 134923 |  |
|  |  |
| Moves and cube decisions: 3 ply |  |
| Confidence No Redouble: | $\pm 0.004(+0.343 . . .+0.352)$ |
| Confidence Redouble: | $\pm 0.007(+0.356 \ldots+0.371)$ |
| Double Decision confidence: | :100.0\% |
| Take Decision confidence: | 100.0\% |
| Duration: 1 minute 24 second |  |

eXtreme Gammon Version: 1.21

Now let's give Black some more timing and see what happens.
Position 2A:


Another position everyone should know. This is a borderline drop/take.

| Analyzed in Rollout |  |
| :---: | :---: |
|  |  |
| Player Winning Chances: | 77.71\% (G: 1.92\% B: 0.02 |
| Opponent Winning Chances:22.29\% (G: $1.23 \%$ B: $0.04 \%$ ) |  |
| Double/Take |  |
| Player Winning Chances: | 77.78\% (G: 1.97\% B: 0.02\%) |
| Opponent Winning Chances:22.22\% (G: $1.19 \% \mathrm{~B}: 0.03 \%$ ) |  |
| Cubeless Equities |  |
| No Redouble: | +0.561 |
| Redouble: | +1.127 |
| Cubeful Equities |  |
| No Redouble: | +0.749 (-0.251) |
| Redouble/Take: | +1.007 (+0.007) |
| Redouble/Drop: | +1.000 |
| Best Cube action: Redouble / Drop |  |
| Rollout details |  |
| 2592 Games rolled with Variance Reduction. Dice Seed: 134923 |  |
|  |  |
| Moves and cube decisions: 3 ply |  |
| Confidence No Redouble: | $\pm 0.007(+0.742 \ldots+0.756)$ |
| Confidence Redouble: ${ }_{\text {Double Decision confidence: }} \mathbf{1 0 0 . 0 \%} 0$ 0.008 (+0.999... +1.014 ) |  |
|  |  |
| Take Decision confidence: | 95.5\% |
| Duration: 1 minute 14 seconds |  |

## Position 2B:



Undiversifying the checkers doesn't change things. The major thing here is the pip count. That makes this easy to remember also: with 20 pips in the outfield, it's a borderline decision. Let's test out our theory by putting one of those checkers into the inner board.

```
Analyzed in Rollout
No Double
Player Winning Chances: 77.62% (G: 1.94% B: 0.02%)
Opponent Winning Chances:22.38% (G: 1.02% B: 0.03%)
Double/Take
Player Winning Chances: 77.72% (G: 1.98% B: 0.03%)
Opponent Winning Chances:22.28% (G: 1.01% B: 0.03%)
Cubeless Equities
No Redouble: +0.561
Redouble: +1.128
Cubeful Equities
No Redouble: +0.751 (-0.249)
Redouble/Take: +1.007 (+0.007)
Redouble/Drop: +1.000
Best Cube action: Redouble / Drop
Rollout details
2592 Games rolled with Variance Reduction.
Dice Seed: }13492
Moves and cube decisions: 3 ply
Confidence No Redouble: }\pm0.007(+0.744\ldots+0.758
Confidence Redouble: }\quad\pm0.008(+0.999\ldots+1.015
Double Decision confidence: 100.0%
Take Decision confidence: 96.4%
Duration: 57.7 seconds
```


## Position 2C:



With a checker on the 16 and a checker on the 4 , we have a definite take. What happened? It isn't obvious.


## Position 2D:



With one on the 15 and one on the 5, we're back to a borderline decision. What about the 14 and 6 ?

Analyzed in Rollout
No Double
Player Winning Chances: $\quad 77.75 \%$ (G: $1.93 \%$ B: $0.02 \%$ )
Opponent Winning Chances:22.25\% (G: $1.04 \%$ B: 0.03\%)
Double/Take
Player Winning Chances: $\quad 77.87 \%$ (G: $1.97 \%$ B: $0.03 \%$ )
Opponent Winning Chances:22.13\% (G: $1.02 \%$ B: $0.03 \%$ )
Cubeless Equities
No Redouble: $\quad+0.564$
Redouble: +1.134
Cubeful Equities
No Redouble: $\quad+0.752(-0.248)$
Redouble/Take: $\quad+1.009$ (+0.009)
Redouble/Drop: +1.000
Best Cube action: Redouble / Drop

## Rollout details

2592 Games rolled with Variance Reduction.
Dice Seed: 134923
Moves and cube decisions: 3 ply
Confidence No Redouble: $\pm 0.007(+0.745 \ldots+0.759)$
Confidence Redouble: $\quad \pm 0.008(+1.002 \ldots+1.017)$
Double Decision confidence: 100.0\%
Take Decision confidence: 99.2\%
Duration: 53.8 seconds

## Position 2E:



Back to borderline again. The key here seems to be that the 5 point is the best place to have a checker in these kinds of positions. Putting a checker on the 6 point with this much timing is almost as good because one of the checkers is likely to end up on the 5 point, whereas a checker on the 4 point can never land on the 5 point.

```
Analyzed in Rollout
No Double
Player Winning Chances: 77.55% (G: 1.93% B: 0.03%)
Opponent Winning Chances:22.45% (G: 1.22% B: 0.04%)
Double/Take
Player Winning Chances: 77.59% (G: 1.97% B: 0.03%)
Opponent Winning Chances:22.41% (G: 1.23% B: 0.04%)
Cubeless Equities
No Redouble: +0.558
Redouble: +1.118
Cubeful Equities
No Redouble: +0.743 (-0.248)
Redouble/Take: +0.991
Redouble/Drop: +1.000 (+0.009)
Best Cube action: Redouble / Take
Rollout details
2 5 9 2 \text { Games rolled with Variance Reduction.}
Dice Seed: }13492
Moves and cube decisions: 3 ply
Confidence No Redouble: }\quad\pm0.007(+0.736\ldots+0.750
Confidence Redouble: }\quad\pm0.008(+0.984\ldots+0.999
Double Decision confidence: 100.0%
Take Decision confidence: 98.9%
Duration: 54.7 seconds
eXtreme Gammon Version: 1.21
```

Position 2F:


Again pip count is by far the major factor rather than placement of spares. If we modify Position 2C to add a pip of timing we reach a clear pass.

```
Analyzed in Rollout
No Double
Player Winning Chances: 78.10% (G: 1.97% B: 0.02%)
Opponent Winning Chances:21.90% (G: 1.21% B: 0.03%)
Double/Take
Player Winning Chances: 78.29% (G: 2.01% B: 0.03%)
Opponent Winning Chances:21.71% (G: 1.17% B: 0.03%)
Cubeless Equities
No Redouble: +0.569
Redouble: +1.148
Cubeful Equities
No Redouble: +0.762 (-0.238)
Redouble/Take: +1.027 (+0.027)
Redouble/Drop: +1.000
Best Cube action: Redouble / Drop
Rollout details
2592 Games rolled with Variance Reduction.
Dice Seed: }13492
Moves and cube decisions: 3 ply
Confidence No Redouble: }\pm0.007(+0.755\ldots+0.769
Confidence Redouble: }\pm0.008(+1.020\ldots..+1.035
Double Decision confidence: 100.0%
Take Decision confidence: 100.0%
Duration: 46.0 seconds
```

This is mostly familiar stuff, but let's get beyond simple material and mix it up a bit by adding blots to the picture.

## Position 3A:



With a blot in the outfield it's a bit different. Here it's a big redouble/take even though the pips are about the same as before and Black has no additional checkers or time to go after the White blot. White's blot is in the worst place in the outfield, other than his own bar. Note that Black wins $17 \%$ gammons from here. Everyone should know that if he picks up the other blot he wins about $40 \%$ gammons, but even if he escapes and misses as he comes into the home board, he still wins somewhere between about $17 \%$ and $21 \%$, depending on the nature of the spares. With all 3 spares on the ace point he still wins $11 \%$ gammons.

| Analyzed in Rollout |  |
| :---: | :---: |
| No Double |  |
| Player Winning Chances: | 68.33\% (G: 17.48\% B: 0.27\%) |
| Opponent Winning Chances: | :31.67\% (G: 1.84\% B: 0.05\%) |
| Double/Take |  |
| Player Winning Chances: | 69.20\% (G: 17.06\% B: 0.24\%) |
| Opponent Winning Chances: | :30.79\% (G: 1.69\% B: 0.05\%) |
| Cubeless Equities |  |
| No Redouble: | +0.525 |
| Redouble: | +1.080 |
| Cubeful Equities |  |
| No Redouble: | +0.585 (-0.279) |
| Redouble/Take: | +0.865 |
| Redouble/Drop: | +1.000 (+0.135) |
| Best Cube action: Redouble / Take |  |
| Rollout details |  |
| 2592 Games rolled with Variance Reduction. |  |
| Dice Seed: 134923 |  |
| Moves and cube decisions: 3 ply |  |
| Confidence No Redouble: | $\pm 0.006(+0.579 \ldots+0.591)$ |
| Confidence Redouble: | $\pm 0.008(+0.857 \ldots+0.873)$ |
| Double Decision confidence: | : 100.0\% |
| Take Decision confidence: | 100.0\% |
| Duration: 2 minutes 49 secon | nds |

## Position 3B:



With a blot occupying the back of the prime, it's much worse for White. This position, which would barely be a redouble if White's blot were moved to the 3 point (going by Position 1G), is getting close to a drop.

```
Analyzed in Rollout
No Double
Player Winning Chances: 66.69% (G: 23.65% B: 0.54%)
Opponent Winning Chances:33.31% (G: 1.60% B: 0.04%)
Double/Take
Player Winning Chances: 67.24% (G: 23.18% B: 0.52%)
Opponent Winning Chances:32.76% (G: 1.58% B: 0.04%)
Cubeless Equities
No Redouble: +0.559
Redouble: +1.131
Cubeful Equities
No Redouble: +0.641 (-0.296)
Redouble/Take: +0.937
Redouble/Drop: +1.000 (+0.063)
Best Cube action: Redouble / Take
```


## Rollout details

```
2592 Games rolled with Variance Reduction.
Dice Seed: 134923
Moves and cube decisions: 3 ply
Confidence No Redouble: \(\quad \pm 0.009(+0.632 \ldots+0.650)\)
Confidence Redouble: \(\quad \pm 0.010(+0.927 \ldots+0.948)\)
Double Decision confidence: 100.0\%
Take Decision confidence: \(\quad 100.0 \%\)
Duration: 1 minute 49 seconds
```


## Position 3C:



With one more pip now it's a big pass. So, with 10 pips in the inner board, it's the point of last take.

```
Analyzed in Rollout
No Double
Player Winning Chances: 69.18% (G: 25.32% B: 0.57%)
Opponent Winning Chances:30.82% (G: 1.60% B: 0.04%)
Double/Take
Player Winning Chances: 69.39% (G: 25.03% B: 0.54%)
Opponent Winning Chances:30.61% (G: 1.52% B: 0.04%)
Cubeless Equities
No Redouble: +0.626
Redouble: }+1.25
Cubeful Equities
No Redouble: }\quad+0.733(-0.267
Redouble/Take: +1.077 (+0.077)
Redouble/Drop: +1.000
Best Cube action: Redouble / Drop
Rollout details
2 5 9 2 \text { Games rolled with Variance Reduction.}
Dice Seed: }13492
Moves and cube decisions: 3 ply
Confidence No Redouble: }\pm0.010(+0.723...+0.742
Confidence Redouble: }\quad\pm0.011(+1.066\ldots+1.087
Double Decision confidence: 100.0%
Take Decision confidence: 100.0%
Duration: }1\mathrm{ minute 24 seconds
```



An interesting little factoid is that of the possible 11 pip configurations, the 8 and 3 is the worst. In fact, it's bad enough that it's a clear take still. No other 11 pip configuration is better than a borderline pass. The reason seems to be that it can't handle 54, 53, and 44 breaks two points.

```
Analyzed in Rollout
No Double
Player Winning Chances: }\quad67.25% (G: 24.22% B: 0.55%
Opponent Winning Chances:32.75% (G: 2.45% B: 0.07%)
Double/Take
Player Winning Chances: 67.58% (G: 23.87% B: 0.52%)
Opponent Winning Chances:32.42% (G: 2.47% B: 0.07%)
Cubeless Equities
No Redouble: +0.567
Redouble: +1.140
Cubeful Equities
No Redouble: +0.675 (-0.273)
Redouble/Take: +0.948
Redouble/Drop: +1.000 (+0.052)
Best Cube action: Redouble / Take
```


## Rollout details

```
2592 Games rolled with Variance Reduction.
Dice Seed: 134923
Moves and cube decisions: 3 ply
Confidence No Redouble: \(\quad \pm 0.009(+0.666 \ldots+0.685)\)
Confidence Redouble: \(\quad \pm 0.011(+0.937 \ldots+0.960)\)
Double Decision confidence: 100.0\%
Take Decision confidence: 100.0\%
Duration: 1 minute 30 seconds
```


## Position 3E:



With spares on the $7 \& 4$, 44 still breaks two points but it can handle 53 .
Analyzed in Rollout No Double
Player Winning Chances: $\quad 68.19 \%$ (G: $24.86 \%$ B: $0.56 \%$ ) Opponent Winning Chances:31.81\% (G: $1.76 \%$ B: 0.05\%) Double/Take
Player Winning Chances: $\quad 68.53 \%$ (G: $24.43 \%$ B: $0.53 \%$ ) Opponent Winning Chances:31.47\% (G: $1.72 \%$ B: 0.05\%) Cubeless Equities

| No Redouble: | +0.600 |
| :--- | :--- |
| Redouble: | +1.205 |

Cubeful Equities
No Redouble: $\quad+0.703(-0.297)$
Redouble/Take: $\quad+1.020(+0.020)$
Redouble/Drop: +1.000
Best Cube action: Redouble / Drop

## Rollout details

2592 Games rolled with Variance Reduction.
Dice Seed: 134923
Moves and cube decisions: 3 ply
Confidence No Redouble: $\quad \pm 0.009(+0.693 \ldots+0.712)$
Confidence Redouble: $\quad \pm 0.011(+1.009 \ldots+1.031)$
Double Decision confidence: 100.0\%
Take Decision confidence: 100.0\%
Duration: 1 minute 35 seconds
eXtreme Gammon Version: 1.21

Let's look at 2 blot positions.
Position 4A:


With 2 blots strewn in the outfield, it becomes a huge pass really quickly. This was our reference for borderline redouble in Position 1G, here a monster pass.

Analyzed in Rollout<br>No Double<br>Player Winning Chances: $\quad 67.69 \%$ (G: $41.47 \%$ B: $1.45 \%$ )<br>Opponent Winning Chances:32.31\% (G: 2.03\% B: $0.05 \%$ )<br>Double/Take<br>Player Winning Chances: $\quad 66.08 \%$ ( $G: 41.50 \%$ B: $1.39 \%$ )<br>Opponent Winning Chances:33.92\% (G: 1.93\% B: $0.05 \%$ )<br>Cubeless Equities<br>No Redouble: $\quad+0.762$<br>Redouble: $\quad+1.461$<br>Cubeful Equities<br>No Redouble: $\quad+0.922(-0.078)$<br>Redouble/Take: +1.196 (+0.196)<br>Redouble/Drop: +1.000<br>Best Cube action: Redouble / Drop<br>Rollout details<br>2592 Games rolled with Variance Reduction.<br>Dice Seed: 134923<br>Moves and cube decisions: 3 ply<br>Confidence No Redouble: $\quad \pm 0.009(+0.913 \ldots+0.931)$<br>Confidence Redouble: $\quad \pm 0.014(+1.182 \ldots+1.209)$<br>Double Decision confidence: 100.0\%<br>Take Decision confidence: 100.0\%<br>Duration: 2 minutes 36 seconds

## Position 4B:



However, the 2 blots also reaches a high state of volatility. Comparing Positions 1B and 1G, 2 pips meant about . 140 of equity, while here it's worth .170. Escaping becomes better than usual and crashing becomes worse (since you lose out on the opportunity to pick up the blots and win a gammon). That means the cube action becomes much more sensitive to the timing issues. This is our borderline take/drop reference (1 pip better than the initial cube reference in Position 1A).

```
Analyzed in Rollout
No Double
Player Winning Chances: 63.13% (G: 38.57% B: 1.13%)
Opponent Winning Chances:36.87% (G: 1.84% B: 0.05%)
Double/Take
Player Winning Chances: 63.48% (G: 38.32% B: 1.07%)
Opponent Winning Chances:36.52% (G: 1.73% B: 0.04%)
Cubeless Equities
No Redouble: +0.641
Redouble: +1.292
Cubeful Equities
No Redouble: +0.723 (-0.277)
Redouble/Take: +1.018(+0.018)
Redouble/Drop: +1.000
Best Cube action: Redouble / Drop
Rollout details
2 5 9 2 \text { Games rolled with Variance Reduction.}
Dice Seed: }13492
Moves and cube decisions: 3 ply
Confidence No Redouble: }\pm0.010(+0.713\ldots+0.733
Confidence Redouble: }\quad\pm0.012(+1.006\ldots+1.029
Double Decision confidence:100.0%
Take Decision confidence: 99.9%
Duration: 3 minutes 37 seconds
```

Now let's look at 2 checkers to escape. How do they fare?
Position 5A:


Here's another two reference positions that everyone should know. Vs. a perfect configuration like this, 2 checkers to escape will always be a take.

```
Analyzed in Rollout
No Double
Player Winning Chances: 68.89% (G: 25.10% B: 0.61%)
Opponent Winning Chances:31.11% (G: 6.27% B: 0.25%)
Double/Take
Player Winning Chances: 69.01% (G: 24.90% B: 0.60%)
Opponent Winning Chances:30.99% (G: 6.17% B: 0.25%)
Cubeless Equities
No Redouble: +0.570
Redouble: +1.142
Cubeful Equities
No Redouble: +0.695 (-0.233)
Redouble/Take: +0.929
Redouble/Drop: +1.000 (+0.071)
Best Cube action: Redouble / Take
Rollout details
2 5 9 2 \text { Games rolled with Variance Reduction.}
Dice Seed: }13492
Moves and cube decisions: 3 ply
Confidence No Redouble: }\pm0.010(+0.685\ldots+0.706
Confidence Redouble: }\quad\pm0.017(+0.912\ldots+0.945
Double Decision confidence: 100.0%
Take Decision confidence: 100.0%
Duration: 2 minutes 52 seconds
```


## Position 5B:



With 12 pips in the outfield, we have a borderline no redouble.

## Analyzed in Rollout

No Double
Player Winning Chances: $\quad 61.92 \%$ (G: 20.85\% B: 0.48\%)
Opponent Winning Chances:38.08\% (G: 8.18\% B: 0.29\%)
Double/Take
Player Winning Chances: $\quad 61.86 \%$ (G: 20.74\% B: 0.47\%)
Opponent Winning Chances:38.14\% (G: 7.98\% B: 0.31\%)
Cubeless Equities
No Redouble: $\quad+0.367$
Redouble: $\quad+0.733$
Cubeful Equities
No Redouble: $\quad+0.486$
Redouble/Take: $\quad+0.477$ (-0.009)
Redouble/Drop: $\quad+1.000$ (+0.514)
Best Cube action: No Redouble / Take
Rollout details
2592 Games rolled with Variance Reduction.
Dice Seed: 134923
Moves and cube decisions: 3 ply
Confidence No Redouble: $\quad \pm 0.006(+0.480 \ldots+0.492)$
Confidence Redouble: $\pm 0.020(+0.457 \ldots+0.497)$
Double Decision confidence: 80.0\%
Take Decision confidence: $100.0 \%$
Duration: 3 minutes 16 seconds
eXtreme Gammon Version: 1.21

## Position 5C:



If we take away 3 pips timing then we have a borderline initial cube. My guess is a centered cube here is very rare.

```
Analyzed in Rollout
No Double
Player Winning Chances: \(\quad 58.62 \%\) (G: \(18.77 \%\) B: 0.39\%)
Opponent Winning Chances:41.38\% (G: 8.97\% B: 0.33\%)
Double/Take
Player Winning Chances: \(\quad 58.65 \%\) (G: \(18.63 \%\) B: \(0.40 \%\) )
Opponent Winning Chances:41.35\% (G: 8.88\% B: 0.33\%)
Cubeless Equities
No Double: \(\quad+0.271\)
Double: \(\quad+0.542\)
Cubeful Equities
No Double: \(\quad+0.228(-0.023)\)
Double/Take: \(\quad+0.252\)
Double/Drop: \(\quad+1.000(+0.748)\)
Best Cube action: Double / Take
Rollout details
2592 Games rolled with Variance Reduction.
Dice Seed: 134923
Moves and cube decisions: 3 ply
Confidence No Double: \(\quad \pm 0.011(+0.218 \ldots+0.239)\)
Confidence Double: \(\pm 0.020(+0.231 \ldots+0.272)\)
Double Decision confidence: \(97.5 \%\)
Take Decision confidence: 100.0\%
Duration: 4 minutes 42 seconds
```

eXtreme Gammon Version: 1.21

Position 5D:


If we back the prime up a pip we can take away a couple of pips of timing and still have a borderline decision due to the increased gammons.

Analyzed in Rollout<br>No Double<br>Player Winning Chances: $\quad 61.06 \%$ (G: $25.20 \%$ B: $0.42 \%$ )<br>Opponent Winning Chances:38.94\% (G: 7.65\% B: $0.29 \%$ )<br>Double/Take<br>Player Winning Chances: $\quad 61.53 \%$ (G: $25.08 \%$ B: $0.42 \%$ )<br>Opponent Winning Chances:38.47\% (G: 7.32\% B: $0.28 \%$ )<br>Cubeless Equities<br>No Redouble: $\quad+0.398$<br>Redouble: +0.819<br>Cubeful Equities<br>No Redouble: $\quad+0.512(-0.009)$<br>Redouble/Take: +0.522<br>Redouble/Drop: $\quad+1.000$ (+0.478)<br>Best Cube action: Redouble / Take<br>Rollout details<br>2592 Games rolled with Variance Reduction.<br>Dice Seed: 134923<br>Moves and cube decisions: 3 ply<br>Confidence No Redouble: $\quad \pm 0.006(+0.507 \ldots+0.518)$<br>Confidence Redouble: $\pm 0.013(+0.508 \ldots+0.535)$<br>Double Decision confidence: 89.8\%<br>Take Decision confidence: 100.0\%<br>Duration: 6 minutes 26 seconds

## Position 5E:



Backing up the prime one more pip and taking away 2 pips timing gives us another borderline decision.

## Analyzed in Rollout

No Double
Player Winning Chances: $\quad 61.08 \%$ (G: $31.10 \%$ B: $0.33 \%$ )
Opponent Winning Chances:38.92\% (G: $7.53 \%$ B: $0.24 \%$ )
Double/Take
Player Winning Chances: $\quad 60.97 \%$ (G: $30.72 \%$ B: $0.34 \%$ )
Opponent Winning Chances:39.03\% (G: $7.59 \%$ B: $0.29 \%$ )
Cubeless Equities
No Redouble: $\quad+0.458$
Redouble: +0.903
Cubeful Equities
No Redouble: $\quad+0.547$
Redouble/Take: $\quad+0.547(-0.001)$
Redouble/Drop: +1.000 (+0.453)
Best Cube action: No Redouble / Take
Rollout details
2592 Games rolled with Variance Reduction.
Dice Seed: 134923
Moves and cube decisions: 3 ply
Confidence No Redouble: $\quad \pm 0.006(+0.541 \ldots+0.554)$
Confidence Redouble: $\quad \pm 0.015(+0.531 \ldots+0.562)$
Double Decision confidence:54.2\%
Take Decision confidence: 100.0\%
Duration: 8 minutes 07 seconds
eXtreme Gammon Version: 1.21

Position 5F:


What if we back up the prime one more pip? Doesn't happen too often, but maybe we can understand something about the nature of the position. Again, being one pip further back is worth about 2 pips of timing in the outfield.

Analyzed in Rollout
No Double
Player Winning Chances: $\quad 58.01 \%$ (G: $37.35 \%$ B: $0.23 \%$ )
Opponent Winning Chances:41.99\% (G: 7.93\% B: 0.29\%)
Double/Take
Player Winning Chances: $\quad 58.43 \%$ (G: $37.47 \%$ B: $0.22 \%$ )
Opponent Winning Chances:41.57\% (G: 8.29\% B: 0.28\%)
Cubeless Equities
No Redouble: $\quad+0.454$
Redouble: $\quad+0.920$
Cubeful Equities
No Redouble: $\quad+0.533$
Redouble/Take: +0.521 (-0.012)
Redouble/Drop: $\quad+1.000$ (+0.467)
Best Cube action: No Redouble / Take
Rollout details
2592 Games rolled with Variance Reduction.
Dice Seed: 134923
Moves and cube decisions: 3 ply
Confidence No Redouble: $\pm 0.009(+0.524 \ldots+0.541)$
Confidence Redouble: $\pm 0.018(+0.503 \ldots+0.539)$
Double Decision confidence: 88.6\%
Take Decision confidence: $\quad 100.0 \%$
Duration: 15 minutes 54 seconds
eXtreme Gammon Version: 1.21

## Position 5G:



But let's remember that the 6 point is one of the worst places to have a checker with very little timing. What if we advance it one pip to the 5 point? Note that although we ostensibly lose a pip of timing, it goes from a borderline no redouble to a borderline redouble.

| Analyzed in Rollout |  |
| :---: | :---: |
|  |  |
| Player Winning Chances: | 58.79\% (G: 36.43\% B: 0.19\%) |
| Opponent Winning Chances:41.21\% (G: 7.47\% B: $0.25 \%$ ) |  |
| Double/Take |  |
| Player Winning Chances: | 59.41\% (G: 37.29\% B: 0.20 |
| Opponent Winning Chances:40.59\% (G: $7.89 \%$ B: $0.24 \%$ ) |  |
| Cubeless Equities |  |
| No Redouble: | +0.465 |
| Redouble: | +0.964 |
| Cubeful Equities |  |
| No Redouble: | +0.541 (-0.027) |
| Redouble/Take: | +0.567 |
| Redouble/Drop: | +1.000 (+0.433) |
| Best Cube action: Redouble / Take |  |
| Rollout details |  |
| 2592 Games rolled with Variance Reduction. <br> Dice Seed: 134923 |  |
|  |  |
| Moves and cube decisions: 3 ply |  |
| Confidence No Redouble: | $\pm 0.009(+0.531 \ldots+0.550)$ |
| Confidence Redouble: | $\pm 0.018(+0.550 \ldots+0.585)$ |
| Double Decision confidence: | :99.6\% |
| Take Decision confidence: | 100.0\% |
| Duration: 16 minutes 01 sec |  |

## Lessons:

With one checker to leap a perfect prime vs. one on the bar, 6 pips is the point of initial cube, 9 pips is the point of redouble, and 20 pips is the point of pass (6/9/20, or 5/8/19 by traditional counting). With two checkers to leap a perfect prime vs. two on the bar, 12 pips is the point of last redouble ( 11 by traditional counting).

Having more checkers back than the opponent is a major disadvantage.
Blot count can make a huge difference in prime vs. prime positions, and can increase the volatility and sensitivity to timing considerations.

For each pip further back the prime is with 2 checkers at the edge, compensate by taking away about 2 pips of timing.

The best place for a spare checker, especially if you don't have very much timing, is the 5 point. In some cases it may even be better to take away a pip of timing to advance the spare to the 5 point.

Next month, we'll look at cube action with checkers that are not at the edge, and where the side cubing has an impure position.

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[^0]:    Analyzed in Rollout
    No Double
    Player Winning Chances: $\quad 58.86 \%$ (G: 1.39\% B: 0.01\%)
    Opponent Winning Chances:41.14\% (G: 1.99\% B: 0.05\%)
    Double/Take
    Player Winning Chances: $\quad 58.95 \%$ (G: 1.45\% B: 0.02\%)
    Opponent Winning Chances:41.05\% (G: 1.96\% B: 0.04\%)
    Cubeless Equities
    No Double: $\quad+0.171$

    Double: $\quad+0.347$
    Cubeful Equities
    No Double: $\quad+0.126(-0.004)$
    Double/Take: $\quad+0.130$
    Double/Drop: $\quad+1.000(+0.870)$
    Best Cube action: Double / Take
    Rollout details
    2592 Games rolled with Variance Reduction.
    Dice Seed: 134923
    Moves and cube decisions: 3 ply
    Confidence No Double: $\quad \pm 0.005(+0.121 \ldots+0.131)$
    Confidence Double: $\quad \pm 0.008(+0.122 \ldots+0.138)$
    Double Decision confidence: $78.6 \%$
    Take Decision confidence: $\quad 100.0 \%$
    Duration: 1 minute 25 seconds

